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$$\mathbb{N}^* \quad n \quad c_n = \sqrt{n-1} - \sqrt{n+1} \quad b_n = \frac{n}{\sqrt{n+1}} \quad a_n = \frac{n}{3^n}$$

:05 •

$$(u_n)_{n \geq 0}$$

$$\begin{cases} u_0 = -\frac{1}{2} \\ u_{n+1} = \frac{2u_n}{1+u_n^2}; n \in \mathbb{N} \end{cases}$$

$$\forall n \in \mathbb{N}; -1 < u_n < 0 \quad \text{—} \quad \text{—}$$

$$-\frac{1}{2} \quad (u_n)_{n \geq 0} \quad \text{—} \quad \text{—}$$

:03 •

$$f \quad u_n = f(n) \quad (u_n)$$

$$[k, +\infty[ \quad f \quad k \in \mathbb{N} \quad [k, +\infty[$$

$$[k, +\infty[ \quad f \quad (u_n)_{n \geq k}$$

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$$\forall n \in \mathbb{N}; u_n = \frac{-2n+5}{n+1} \quad (u_n)_{n \geq 0}$$

$$\Delta = \begin{vmatrix} -2 & 5 \\ 1 & 1 \end{vmatrix} = -7 < 0 \quad f(x) = \frac{-2x+5}{x+1} \quad u_n = f(n)$$

$$\mathbb{R}_+ \subset ]-1, +\infty[ \quad ]-1, +\infty[ \quad f \quad (u_n)_{n \geq 0}$$

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$$r \in \mathbb{R}^* \quad r \quad (u_n)_{n \geq 0}$$

$$\forall n \in \mathbb{N}; u_{n+1} = u_n + r$$

:04 •

$$\forall n \in \mathbb{N}; u_{n+1} = \frac{2u_n + 3}{u_n + 2} \quad u_0 = 1 \quad (u_n)_{n \geq 0}$$

$$1 \quad \sqrt{3} \quad (u_n)_{n \geq 0}$$

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$$(u_n)_{n \geq 0}$$

$$\forall n \in \mathbb{N}; u_{n+1} \geq u_n \quad (u_n)_{n \geq 0}$$

$$\forall n \in \mathbb{N}; u_{n+1} > u_n$$

$$\forall n \in \mathbb{N}; u_{n+1} \leq u_n \quad (u_n)_{n \geq 0}$$

$$\forall n \in \mathbb{N}; u_{n+1} < u_n$$

$$(u_n)_{n \geq 0}$$

\_\_\_\_\_ •

$$(b_n) \quad (a_n)$$

$$\forall n \in \mathbb{N}; b_n = n - 4^n \quad \forall n \in \mathbb{N}^*; a_n = n + \frac{1}{n}$$

$$(b_n) \quad (a_n)$$

:02 •

$$(u_n)_{n \geq 0}$$

$$\forall n \in \mathbb{N}; \frac{u_{n+1}}{u_n} > 1 \quad (u_n)_{n \geq 0}$$

$$\forall n \in \mathbb{N}; \frac{u_{n+1}}{u_n} < 1$$

$$(u_n)_{n \geq 0}$$

$$\forall n \in \mathbb{N}; \frac{u_{n+1}}{u_n} < 1 \quad (u_n)_{n \geq 0}$$

$$\forall n \in \mathbb{N}; \frac{u_{n+1}}{u_n} > 1$$

$S_n = n \times u_0 + \frac{n(n-1)r}{2} : r$   $u_0$   $S_n$  :\_\_\_\_\_ •

**:08** •

$T = 5 + 16 + 27 + \dots + 2007$   $S = 6 + 10 + 14 + \dots + 1002$

$X_n = 1 + 6 + 11 + \dots + (5n + 1) : n$  -ب

$X = 1 + 6 + 11 + \dots + 2006$   
 $r = -2$   $(u_n)_{n \geq 1}$  -ج

$S_{17} = 1513$

$u_{17}$   $u_1$

$S_n = 0 : \mathbb{N}$

**:06** •

$\forall n \in \mathbb{N}; \frac{u_n + u_{n+2}}{2} = u_{n+1} : (u_n)_{n \geq 0}$

**:09** •

$(v_n)_{n \geq 0}$   $(u_n)_{n \geq 0}$

$\forall n \in \mathbb{N}; u_n = 2^n \times v_n$   $\begin{cases} v_0 = -1; v_1 = 1 \\ v_{n+2} = v_{n+1} - \frac{v_n}{4}; \forall n \in \mathbb{N} \end{cases}$

$(u_n)_{n \geq 0}$  -ج

$\mathbb{N}$   $n$   $n$   $v_n$   $u_n$  -ب

:\_\_\_\_\_ - (2)

:\_\_\_\_\_ •

$q \in \mathbb{R}^*$   $q$   $(u_n)_{n \geq 0}$

$\forall n \in \mathbb{N}; u_{n+1} = q \times u_n$

:\_\_\_\_\_ •

$u_n = \frac{2^{3n}}{3^{2n}} : \mathbb{N}$   $n$

$u_0$  و حدها الأول  $q$   $(u_n)_{n \geq 0}$

$(u_n)_{n \geq 0}$   $\forall n \in \mathbb{N}; u_{n+1} = u_n : -$  :\_\_\_\_\_ •

$\forall n \in \mathbb{N}; u_{n+1} - u_n = r : r$   $(u_n)_{n \geq 0}$  -  
 $r > 0$  :  $r$   $(u_n)_{n \geq 0}$   
 $r < 0$

:\_\_\_\_\_ •

$u_n = -5n + 10 : \mathbb{N}$   $n$   
 $r = -5$   $(u_n)_{n \geq 0}$   $\forall n \in \mathbb{N}; u_{n+1} - u_n = -5 : -$   
 $r < 0$

**:06** •

$(E): \cos x + \sin x = 0$   $\mathbb{R}$

$r$

**:04** •

$\forall n \in \mathbb{N}; u_n = u_0 + n \times r : r$   $(u_n)_{n \geq 0}$

$\forall (n, m) \in \mathbb{N}^2 : u_n = u_m + (n - m)r :$

**:07** •

$(v_n)_{n \geq 0}$   $(u_n)_{n \geq 0}$

$\forall n \in \mathbb{N}; u_n = 1 + \frac{1}{v_n}$   $\begin{cases} v_0 = \frac{1}{2} \\ v_{n+1} = \frac{v_n}{1 + 2v_n}; \forall n \in \mathbb{N} \end{cases}$

$u_0$   $r$   $(u_n)_{n \geq 0}$  -ج

$\mathbb{N}$   $n$   $n$   $v_n$   $u_n$  -ب

**:05** •

$n$   $S_n = u_0 + u_1 + \dots + u_{n-1}$   $(u_n)_{n \geq 0}$

$S_n = n \frac{u_0 + u_{n-1}}{2}$   $n \in \mathbb{N}^*$

$\forall (n, m) \in \mathbb{N}^2 / n < m; u_n + u_{n+1} + \dots + u_m = \frac{(m - n + 1) \times (u_n + u_m)}{2}$

$$\cdot \forall n \in \mathbb{N}; u_n \times u_{n+2} = u_{n+1}^2 :$$

**:09** •

$$(u_n)_{n \geq 0}$$

**:11** •

$$: (v_n)_{n \geq 0} \quad (u_n)_{n \geq 0}$$

$$\cdot \forall n \in \mathbb{N}; u_n = v_{n+1} - \frac{v_n}{2} \quad \begin{cases} v_0 = -1; v_1 = 1 \\ v_{n+2} = v_{n+1} - \frac{v_n}{4}; \forall n \in \mathbb{N} \end{cases}$$

$$q \quad (u_n)_{n \geq 0} \quad -\dot{\jmath}$$

$$\cdot \mathbb{N} \quad n \quad n \quad v_n \quad u_n \quad -\dot{\jmath}$$

$$\forall n \in \mathbb{N}; u_n = q^n \times u_0 : \quad q$$

**:07** •

$$(u_n)_{n \geq 0}$$

$$\cdot \forall (n, m) \in \mathbb{N}^2; u_n = q^{n-m} \times u_m :$$

**:10** •

$$: (v_n)_{n \geq 0} \quad (u_n)_{n \geq 0}$$

$$\cdot \forall n \in \mathbb{N}; u_n = 3v_n - 2 \quad \begin{cases} v_0 = 3 \\ v_{n+1} = 1 - \frac{v_n}{2}; \forall n \in \mathbb{N} \end{cases}$$

$$(u_n)_{n \geq 0} \quad -\dot{\jmath}$$

$$\cdot \mathbb{N} \quad n \quad n \quad v_n \quad u_n \quad -\dot{\jmath}$$

**:08** •

$$S_n = u_0 + u_1 + \dots + u_{n-1} \quad q \neq 1 \quad (u_n)_{n \geq 0}$$

$$\cdot S_n = u_0 \times \frac{1-q^n}{1-q} : \quad n \in \mathbb{N}^* \quad n$$

$$\cdot \forall (n, m) \in \mathbb{N}^2 / n < m; u_n + u_{n+1} + \dots + u_m = u_n \frac{1-q^{m-n+1}}{1-q} :$$

**:11** •

$$q \quad u_0 = 512 \quad u_4 = 16 \quad (u_n)_{n \geq 1} \quad -\dot{\jmath}$$

$$S_6$$

$$q = 2 \quad u_1 = 7 \quad (u_n)_{n \geq 1} \quad -\dot{\jmath}$$

$$\cdot u_n \quad S_n = 1785 : \quad \mathbb{N}^*$$

$$: \mathbb{N}^* \quad q = \frac{1}{3} \quad (u_n)_{n \geq 1} \quad -\dot{\jmath}$$

$$\cdot u_1 \quad \begin{cases} u_n = 27 \\ S_n = 3267 \end{cases}$$

$$\cdot \forall n \in \mathbb{N}; x_n = (-2)^n + 3n + 1 : \quad (x_n)_{n \geq 0} \quad -\dot{\jmath}$$

$$\cdot S_n = x_0 + x_1 + \dots + x_n : \quad n$$